

$$1. \lim_{x \rightarrow 2} f(x) = 1$$

$$2. \lim_{x \rightarrow -1} f(x) = DNE$$

3.

$$A2. \lim_{x \rightarrow 0} \frac{(\sqrt{x+4} - 2)}{x} = 0.25$$

x	-0.1	-0.01	-0.001	0	0.001	0.01	0.1
$f(x)$	$f(-.1) = 0.2515823400$	$f(-.01) = 0.2501564000$	$f(-.001) = 0.2500160000$?	$f(.001) = 0.2499840000$	$f(0.01) = 0.2498439000$	$f(.1) = 0.2484567300$

4. $f(x)$ is discontinuous at $x = -1$ because $f(-1) = \text{undefined}$. (Removable)

$f(x)$ is discontinuous at $x = 2$ because $\lim_{x \rightarrow 2} f(x) = DNE$. (Non-Removable)

5. $f(x)$ is discontinuous at $x = 1$ because

$$\lim_{x \rightarrow 1^-} f(x) = -1 \text{ and } \lim_{x \rightarrow 1^+} f(x) = 2$$

which means $\lim_{x \rightarrow 1} f(x) = DNE$.

(Non-Removable)

6. For the proof, choose $\delta = \frac{\epsilon}{2}$.

7. For the proof, choose $\delta = \frac{\epsilon}{7}$ on the interval $2 \leq x \leq 4$.

$$8. f'(x) = \lim_{\Delta x \rightarrow 0} \frac{(f(x + \Delta x) - f(x))}{\Delta x} = 2$$

$$9. f'(x) = \lim_{\Delta x \rightarrow 0} \frac{(f(x + \Delta x) - f(x))}{\Delta x} = 2x - 3$$

$$10. \int_1^4 (2x + 3) dx = \lim_{n \rightarrow \infty} \sum_{i=1}^n f(c_i) \Delta x = 24$$

where: $\Delta x = \frac{3}{n}$ and $c_i = 1 + \frac{3}{n}i$

$$11. \int_0^5 (x^2 - 2x) dx = \lim_{n \rightarrow \infty} \sum_{i=1}^n f(c_i) \Delta x = \frac{50}{3}$$

where: $\Delta x = \frac{5}{n}$ and $c_i = 0 + \frac{5}{n}i$