

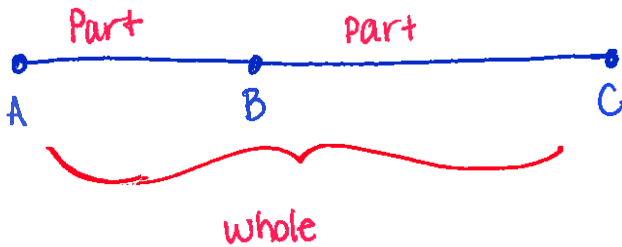
## Segment & Angle Addition

### Segment/Angle Addition Postulates: "Part + Part = Whole"

1. Draw a picture to represent each postulate and identify the "Parts" and the "Whole".

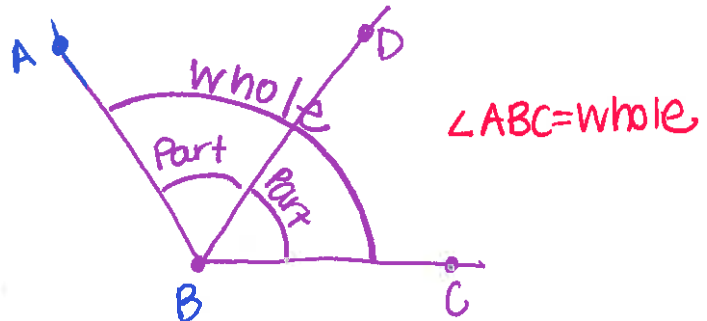
#### Segment Addition Postulate:

If points A, B, and C are *colinear* with B between A and C then  $AB + BC = AC$ .



#### Angle Addition Postulate:

If point D is in the interior of  $\angle ABC$ , then  $m\angle ABD + m\angle DBC = m\angle ABC$ .



**Properties of Equality:** These properties will support our Angle & Segment Addition postulates.

#### Addition

$$\text{If } A=B, \text{ then } A+x = B+x$$

"add x to both sides"

#### Subtraction

$$\text{If } A+x = B+x, \text{ then } A=B$$

"subtract x from both sides"

#### Substitution

$$\text{If } A=B \text{ and } A+x = C, \text{ then } B+x = C$$

"replaced A with B"

#### Reflexive

$$A = A$$

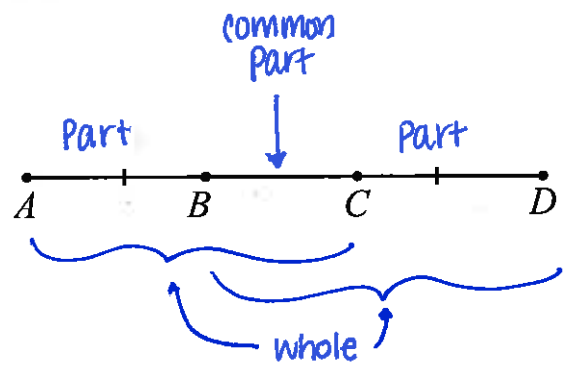
"something is equal to itself."

## The Addition Method: "Going from Small to Big"

2. Example: In this example, two equal parts are connected by a **common part**.

Given:  $\overline{ABCD}$   
 $\overline{AB} \cong \overline{CD}$  Equal Parts (Small)

Prove:  $\overline{AC} \cong \overline{DB}$  Equal Wholes (Big)

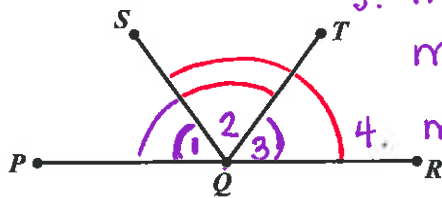


|                             | Statements   | Reasons                  |
|-----------------------------|--|--------------------------|
| (Part = Part)               | 1. $\overline{ABCD}$<br>$\overline{AB} \cong \overline{CD}; AB = CD$ | 1. Given                 |
| (Part + Part = Part + Part) | 2. $\underline{AB + BC = BC + CD}$                                   | 2. add prop. of equality |
| (Parts = Whole)             | 3. $\underline{AB + BC = AC}$<br>$\underline{BC + CD = BD}$          | 3. segment addition      |
| (Whole = Whole)             | 4. $\underline{AC = BD}; \overline{AC} \cong \overline{BD}$          | 4. Substitution.         |

3. Example:

Given:  $\angle PQS \cong \angle RQT$

Prove:  $\angle PQT \cong \angle RQS$

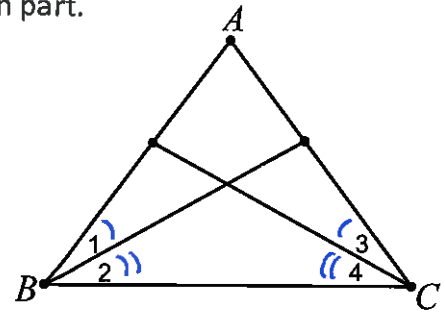


| statements  | Reasons            |
|---|--------------------|
| 1. $\angle PQS \cong \angle RQT; m\angle 1 = m\angle 3$                           | 1. Given           |
| 2. $m\angle 1 + \underline{m\angle 2} = \underline{m\angle 2} + m\angle 3$        | 2. add prop of eq. |
| 3. $m\angle 1 + m\angle 2 = m\angle PQT$<br>$m\angle 2 + m\angle 3 = m\angle RQS$ | 3. Angle Addition  |
| 4. $m\angle PQT = m\angle RQS;$<br>$\angle PQT \cong \angle RQS$                  | 4. Substitution    |

4. Example: In this example equal parts are not connected by a common part.

Given:  $\angle 1 \cong \angle 3$   
 $\angle 2 \cong \angle 4$  ← Equal Parts (Small)

Prove:  $\angle ABC \cong \angle ACB$  ← Equal Wholes (Big)

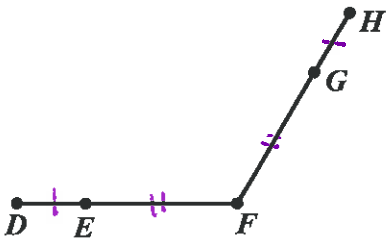


|                             | Statements  | Reasons             |
|-----------------------------|---|---------------------|
| (Part = Part)               | 1. $\angle 1 \cong \angle 3 ; m\angle 1 = m\angle 3$              | 1. Given            |
| (Part = Part)               | $\angle 2 \cong \angle 4 ; m\angle 2 = m\angle 4$                 |                     |
| (Part + Part = Part + Part) | 2. $m\angle 1 + m\angle 2 = m\angle 3 + m\angle 4$                | 2. add prop of eq   |
|                             | 3. $m\angle 1 + m\angle 2 = m\angle ABC$                          | 3. Segment Addition |
| (Parts = Whole)             | 4. $m\angle 3 + m\angle 4 = m\angle ACB$                          | 4. Segment Addition |
| (Whole = Whole)             | 5. $m\angle ABC = m\angle ACB ;$<br>$\angle ABC \cong \angle ACB$ | 5. Substitution     |

5. Example:

Given:  $\overline{DE} \cong \overline{HG}$   
 $\overline{GF} \cong \overline{EF}$

Prove:  $\overline{DF} \cong \overline{HF}$



- ①  $\overline{DE} \cong \overline{HG} ; DE = HG$       ① Given
- ②  $\overline{GF} \cong \overline{EF} ; GF = EF$       ② add prop of equality
- ③  $DE + EF = DF$   
 $HG + GF = HF$       ③ segment addition
- ④  $DF = HF ; \overline{DF} \cong \overline{HF}$       ④ substitution

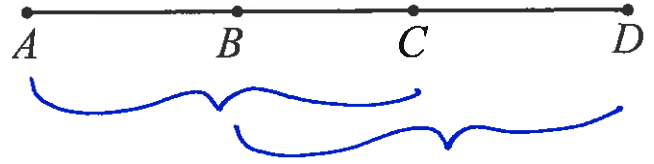
## The Subtraction Method: "Going from Big to Small"

There is **NO** segment/angle subtraction postulate!

6. Example:

Given:  $\overline{ABCD}$   
 $\overline{AC} \cong \overline{DB}$  Equal Wholes (Big)

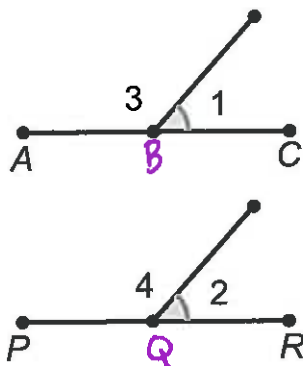
Prove:  $\overline{AB} \cong \overline{CD}$  Equal Parts (Small)



|                             | Statements                                       | Reasons                        |
|-----------------------------|--|--------------------------------|
|                             | 1. $\overline{ABCD}$                             | 1. <u>given</u>                |
| (Whole = Whole)             | $\overline{AC} \cong \overline{DB} ; AC = DB$    |                                |
| (Parts = Whole)             | 2. $AC = AB + BC$<br>$BD = BC + CD$              | 2. <u>segment addition</u>     |
| (Part + Part = Part + Part) | 3. $AB + BC = BC + CD$                           | 3. <u>substitution (subst)</u> |
| (Part = Part)               | 4. $AB = CD ; \overline{AB} \cong \overline{CD}$ | 4. <u>subtr. prop of eq.</u>   |

7. Use the **Subtraction Method** to complete the proof of the following theorem:

"If 2 angles are congruent, then their supplements are congruent."



| Statement   | Reason   |
|---|--|
| 1. $\angle 1 \cong \angle 2$ ;<br>$\angle ABC = 180$ ; $\angle PQR = 180$ | 1. Given   |
| 2. $m\angle ABC = m\angle PQR$  | 2. <u>straight</u><br><u>supp Ls have 180°</u>                 |
| 3. $m\angle 1$ supp $m\angle 3$<br>$m\angle 2$ supp $m\angle 4$           | 3. <u>adj Ls that form a straight</u><br><u>line are supp.</u> |
| 4. $m\angle 1 + m\angle 3 = 180$<br>$m\angle 2 + m\angle 4 = 180$         | 4. <u>Supp Ls have 180°</u>                                    |
| 5. $m\angle 1 + m\angle 3 = m\angle 2 + m\angle 4$                        | 5. <u>substitution</u>   |
| * 6. $m\angle 1 + m\angle 3 = m\angle 1 + m\angle 4$                      | 6. <u>substitution</u>   |
| 7. $\angle 3 \cong \angle 4$  | 7. <u>subtr. prop of eq.</u>                                   |